

Can Prospect Theory Explain Risk-Seeking Behavior by Terminally Ill Patients?

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Running Head: Risk-Seeking by Terminally Ill Patients

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1 **Abstract**

2 Patients with life-threatening conditions sometimes appear to make risky treatment
3 decisions as their condition declines, contradicting the risk-averse behavior predicted by
4 expected utility theory. Prospect theory accommodates such decisions by describing how
5 individuals evaluate outcomes relative to a reference point and exhibit risk-seeking behavior over
6 losses relative to that point. We show that a patient’s reference point for his or her health is a key
7 factor in determining which treatment option the patient selects, and we examine under what
8 circumstances the more risky option is selected. We also argue that patients’ demand for health
9 care changes as their prognosis worsens, with implications for predicting under what
10 circumstances a patient may select experimental or conventional therapies, or no treatment.

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12 **Keywords**

13 Decision Theory; Life Expectancy; Risk-Taking; Terminally Ill

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Considerable evidence suggests that the standard model of expected utility, though convenient for its mathematical tractability, is inconsistent with observed human behavior. Individuals appear to show preferences over changes in value relative to a reference point, rather than over absolute levels of value. People exhibit risk-seeking behavior under certain conditions (e.g., for small or medium-sized losses) in violation of the concavity assumption of expected utility theory (EU).

Researchers have developed several alternative models of human preferences to explain systematic violations of EU. Among the most well-known models are rank-dependent EU, regret theory, and prospect theory. Perhaps the most widely accepted of these models is prospect theory,^{1,2} which has been applied in a broad range of decision-making contexts, including economics, law, politics, and health care. In this paper, we demonstrate that risk-seeking treatment choices by patients with life-threatening conditions—some of whom select experimental therapies rather than conventional therapies—are consistent with prospect theory preferences. We also show that identification of a patient’s reference point is critical in determining whether the patient will choose riskier or more traditional treatments.

Prospect Theory

Since the development of prospect theory in 1979, a considerable literature has arisen that seeks to explain a broad range of human behavior using the theory’s tenets. (See Hastie and Dawes³ for a detailed review.) Most of this research relates to decision making in business and economics; research in medical decision making typically assumes that patients are always risk-averse.^{4,5} However, the medical literature does contain a few recent studies that draw on concepts

1 of prospect theory. Yaniv⁶ compares predictions of prospect theory, EU, and regret theory to the
2 dilemma faced by physicians who must decide how much information to disclose to critically ill
3 patients. Lenert et al.⁷ demonstrate how the prospect theory value function might explain why
4 patients and the general public report different preferences for health conditions. There is also
5 anecdotal evidence suggesting that patients may become risk-seeking as health declines⁸ and
6 may even make treatment decisions that their physicians report they would not make
7 themselves.^{9,10} For example, some patients with cancer choose aggressive or investigational
8 treatment rather than conventional therapy, even though the former carries greater risk of
9 morbidity.⁶

10 In this paper, we consider patients' treatment choices assuming prospect theory
11 preferences, in which risk-seeking behavior depends on the location of the reference point
12 between gains and losses, rather than on values for each treatment outcome.

13

14 Reference Points

15 Our first task is to identify an appropriate outcome metric for the reference point. In
16 economics, the reference point is typically chosen over wealth or other monetary equivalents. It
17 is less clear how to measure "value" in health care, as there may be several determining factors
18 (e.g., length of life, quality of life). Current health status is often used as the default reference
19 point (e.g., Lenert et al.⁷), although the "aspiration level of survival" may also be appropriate.¹¹
20 In this paper, we assume that prospect theory "values" are measured with respect to a single
21 attribute—life expectancy. There is also evidence that a patient's reference point for life
22 expectancy (or prognosis) evolves, both over time and in response to new information about the
23 patient's health. Dolan¹² found that both current and past health influenced valuation as

1 measured by EuroQol scores, although he also observed that the impact of past illness weakened
2 significantly over time. There is also direct empirical evidence of reference-level shifts within
3 individual patients. For example, Christiansen-Szalanski¹³ found that pregnant women’s views of
4 anesthesia during labor changed according to whether the patient was experiencing labor pain.

5 Although diagnosis of a life-threatening condition may result in an immediate and
6 significant decrease in life expectancy, the patient’s reference point may respond slowly as the
7 patient comes to terms with the change in prognosis. We propose that the patient’s reference
8 point varies in connection with his or her emotional state. We hypothesize that a newly
9 diagnosed patient experiences a period of “recalibration” of life expectancy, in parallel with his
10 or her emotional journey through grief,^{14,15} and that the patient’s reference level for remaining
11 years of life decreases throughout this period. Depending on how long the emotional journey
12 takes, it is reasonable to suppose that the patient’s life-expectancy reference level may lie
13 anywhere between its prediagnosis peak and its disease-acceptance trough at a time when the
14 patient must make a significant treatment choice. A patient who has had multiple occurrences of
15 cancer, on the other hand, may not react to a recurrence of cancer with the same emotions as
16 those felt at an initial diagnosis.⁹ Furthermore, the patient’s reference point may already be
17 reasonably well-calibrated to more realistic levels.¹⁰

18 The prospect theory model of individuals’ preferences replaces the standard concave
19 utility function with a value function that measures changes relative to a reference point. The
20 value function is concave over gains and convex over losses and is steeper in the domain of
21 losses. The prospect theory value function is parameterized as follows:

$$22 \quad v(x) = \begin{cases} (x)^\alpha & x \geq 0 \\ (-\lambda)(-x)^\alpha & x < 0 \end{cases} \quad (1)$$

1 where x is the outcome gain or loss relative to the reference point, λ is the coefficient of loss
2 aversion (i.e., the extent to which individuals are more sensitive to losses relative to gains of equal
3 magnitude), and α is the curvature of the utility function.

4 5 Implications of a Shifting Reference Point

6 We provide a simple graphical example to motivate the analysis that follows. In Figure 1,
7 we compare the value function of a patient who has been diagnosed recently with a life-
8 threatening condition and was previously in full health with a life expectancy of 30 years to that
9 of a patient with a similar medical condition but whose reference point is now calibrated to more
10 realistic levels. As discussed above, we use life expectancy as a proxy for prognosis.

11 The left-hand panel of Figure 1 shows the prospect theory value function for the recently
12 diagnosed patient, whose prognosis reference point equals the prediagnosis life expectancy
13 (approximately 30 years). For this patient, all other prognoses are viewed as losses; hence, the
14 value function is convex and is steepest (i.e., has greatest marginal utility) close to the current
15 reference point. The right-hand panel of Figure 1 shows the value function for a terminally ill
16 patient who has had some time to adapt to his or her condition and whose life expectancy
17 reference point is 5 years. Note that this reference point may or may not equal actual life
18 expectancy, depending on how recently the patient was diagnosed, the patient's health before the
19 recent diagnosis, and other factors that influence the extent to which the patient has "adapted" to
20 current life expectancy.

21 The key to understanding the implications of moving reference points lies in the
22 measurement of relative values of life-expectancy outcomes. To demonstrate this point, we will
23 compare value differences between a pair of relatively low life expectancies (2 and 4 years) and

1 two higher values (14 and 20 years). Note that, for the recently diagnosed patient (left-hand
2 panel in Figure 1), the difference in value between life expectancies of 2 and 4 years is very
3 small (as shown on the vertical axis), whereas the difference in value between 14 and 20 years is
4 greater, because those values are closer to the patient's reference point. This is an example of the
5 diminishing sensitivity of the prospect theory value function. With an expected life span of 30
6 years, this patient views both a 2-year life span and a 4-year life span as having little value but
7 does not distinguish greatly between them. For the patient who has had some time to adapt to his
8 or her condition, the value difference between 2 and 4 years is much greater, because those life
9 expectancies are closer to the patient's current reference point (5 years), whereas the difference
10 between 14 and 20 years is small, because those life expectancies are far from the patient's
11 reference point.

12

13 **Patient Decision Making Under Prospect Theory and EU**

14 In this section, we calibrate patient decision making to the prospect theory value function
15 and compare optimal choices under different reference point assumptions to those made by EU
16 maximizers (who are assumed to have power utility functions with risk-aversion coefficient γ).
17 We consider a hypothetical patient—a 50-year-old woman who has been diagnosed recently with
18 inflammatory breast cancer and has thus experienced a significant negative change in her clinical
19 diagnosis. Before diagnosis, the patient was expected to live to age 78. She now has a 5-year life
20 expectancy without treatment. We assume for simplicity that the patient faces two treatment
21 options—investigational (such as a phase 1 clinical trial) and conventional (standard
22 chemotherapy).

1 Using life expectancy as a quantitative proxy for prognosis, we simplify the analysis
2 further by considering only two mutually exclusive outcomes for the active treatment options—
3 success, in which life expectancy is restored to some proportion of the life expectancy before the
4 recent clinical change, and failure, in which treatment toxicity further reduces life expectancy.
5 Conventional therapy is assumed to have a 25% probability of success and, if successful, would
6 restore 50% of the patient’s prediagnosis life expectancy (i.e., she would expect to live another
7 14 years). However, side effects from conventional therapy, if unsuccessful, would reduce
8 current life expectancy to 4 years.

9 The patient’s oncologist has also informed her that there is an investigational study
10 relating to her type of cancer and that she would likely qualify as a candidate for the
11 experimental therapy. The investigational therapy also offers a 25% success probability and, if
12 successful, would restore 70% of previous life expectancy (i.e., she would be expected to live
13 approximately 20 years). However, side effects from experimental therapy are much more
14 severe. If treatment is unsuccessful, the patient will likely die in about 2 years. (For purposes of
15 the analysis, we assume individuals are calibrated correctly to the “objective” probabilities given
16 in the example.)

17

18 Results

19 Assuming prospect theory preferences with $\alpha = 0.7$ and $\lambda = 2$ (Equation 1), we calculate
20 the patient’s prospective value for each option for a range of reference points. We find that, as
21 the reference point increases, the prospective value of the investigational therapy improves
22 relative to conventional therapy. For reference points greater than approximately 13 years, the

1 patient under prospect theory would choose investigational therapy, “gambling” on the 25%
2 probability of restoring life expectancy to somewhat near prediagnosis levels (Figure 2).

3 Under EU, however, conventional therapy is always preferable to the investigational
4 therapy. Indeed, we need not calculate the utility values in this case; it is enough to observe that
5 the probability-weighted expected value of the conventional therapy is 6.5 years, higher than that
6 of the investigational therapy (6.4 years). Thus, even if the patient is risk-neutral, she will select
7 the conventional therapy under EU. Given any level of risk-aversion, of course, this lower-risk
8 choice is reinforced by the concavity of the patient’s utility function.

9

10 **Discussion**

11 Prospect theory has been used to explain violations of normative EU in a broad range of
12 circumstances. We applied one of the key predictions of prospect theory—that people are risk-
13 seeking in the domain of losses—to explain why some terminally ill patients make risky
14 treatment decisions. The model is flexible enough to permit different decisions by patients with
15 similar treatment outcome possibilities, based on their subjective selection of a “reference point”
16 between gains and losses. We propose that the reference point differs among patients depending
17 on prediagnosis and postdiagnosis life expectancies and also varies for a given patient over time,
18 in parallel with the emotional progression through grief over the diagnosis. (Of course, many
19 other factors may affect patients’ emotional responses to significant medical change and hence
20 their reference points, such as family and career concerns, income and wealth, and so on.)

21 Our analysis has implications for predicting under what circumstances a patient may
22 select experimental or conventional therapies, or no treatment. The findings may be useful for
23 physicians, who have the difficult task of deciding how much information to provide and which

1 treatment option(s) to suggest after diagnosis. For example, Langer¹⁶ notes that, in the case of
2 breast cancer, “many women are unprepared or unable to optimize adjuvant treatment decisions
3 while experiencing the shock and dismay that often follow the confirmation of [the] diagnosis.”
4 An understanding of how a patient’s treatment choices may change over time, as a function both
5 of the magnitude of the change in life expectancy and the patient’s current emotional state, may
6 be of great help to physicians.

7 There are also implications for recruitment into early-phase clinical trials. Experimental
8 therapies are considered highly risky, with low success probabilities, and recruiting patients can
9 be a slow and difficult process. A better understanding of the circumstances in which patients
10 might make risk-seeking choices would be of considerable value to clinical researchers.

11 Our hypothetical calibration of the prospect theory value function also makes a number
12 of assumptions and leaves many questions unanswered. For example, we assume that the
13 patient’s reference level is bounded above by prediagnosis life expectancy and below by the
14 postdiagnosis level assuming no treatment, but we have offered no analytic framework for how
15 the level changes over time. We also leave open the question of how to elicit a consistent
16 measure of a patient’s view of his or her prognosis and ignore the important issue of adjusting
17 for patient bias in judgment of treatment success probabilities. We leave analysis of these issues
18 to future research.

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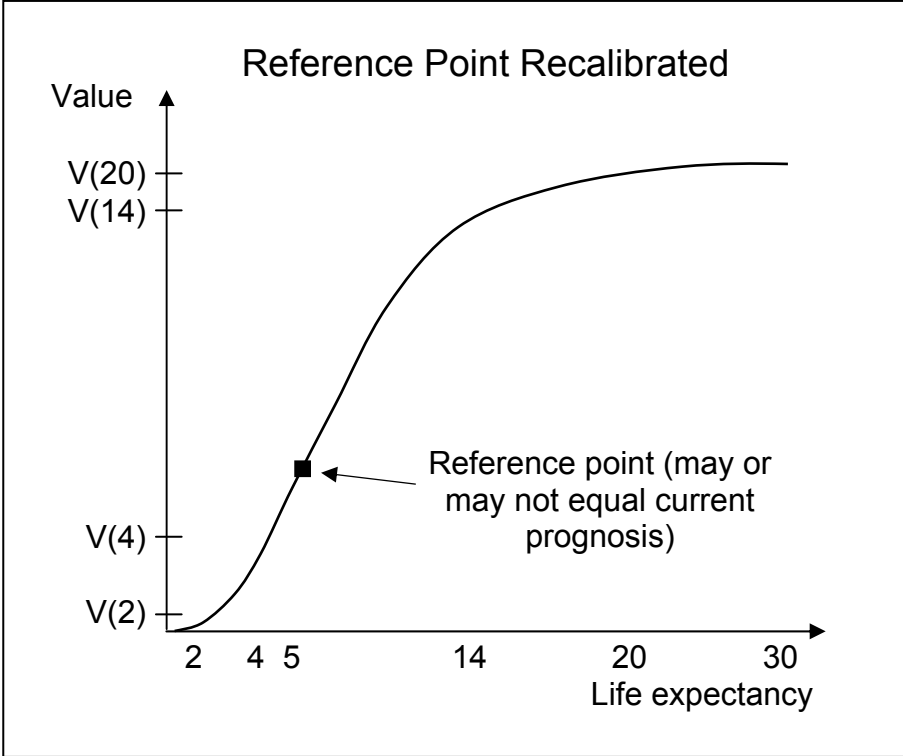
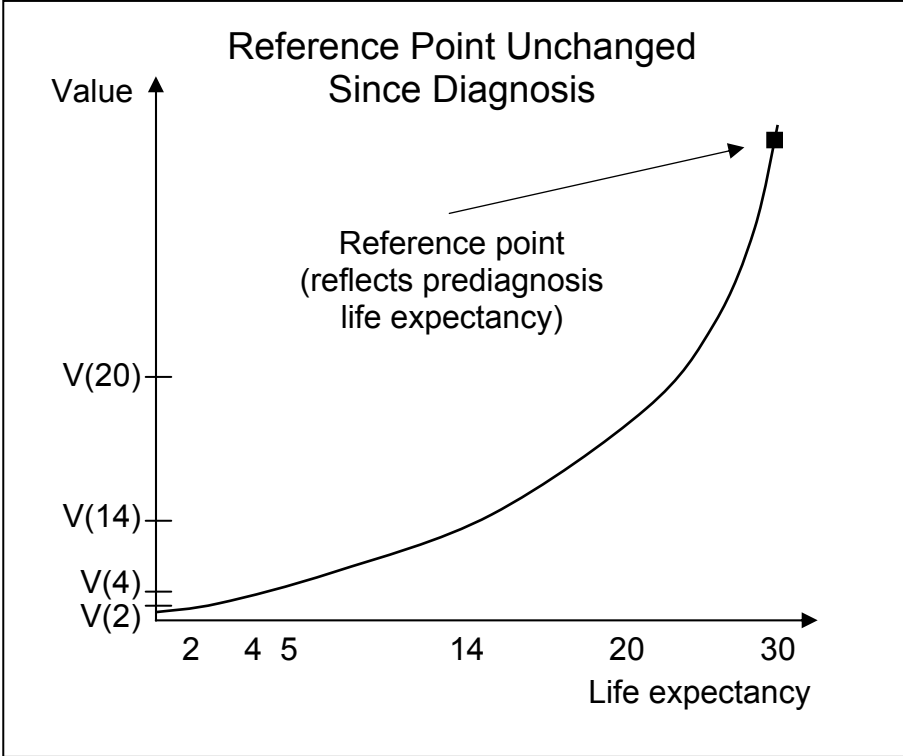
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Figure Legends

Figure 1. Prospect theory value functions for two patients with a life-threatening illness given different reference points.

Figure 2. Prospect theory utility (“prospective value”) for different treatment options given different reference points.



Prospect Theory Utility given different Reference Points
for alternative Treatment Options

